



n -DISTRIBUTIVE NEARLATTICES

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Abstract

For a neutral element $n \in L, [III]$ have introduced the concept of n -distributive lattices which is a generalization of both 0-distributive and 1-distributive lattices. For a central element n of a nearlattice S , we have discussed n -distributive nearlattices which is a generalization of both 0-distributive semilattices and n -distributive lattices. For an element n of nearlattice S , a convex subnearlattice of S containing n is called an n -ideal of S . In this paper, we have given some properties of n -distributive nearlattices. Finally, we have included a generalization of prime Separation Theorem in terms of annihilator n -ideal.

Keywords: Central element, 0-distributive lattice, n -distributive lattice, n -annihilator, annihilator n -ideal, prime n -ideal, n -distributive nearlattice.

I. Introduction

J.C. Varlet has given the concept of 0-distributive and 1-distributive lattices. A lattice L with 0 is called 0-distributive if for all $a, b, c \in L$, $a \wedge b = 0 = a \wedge c$ imply $a \wedge (b \vee c) = 0$. Similarly, a lattice L with 1 is called 1-distributive if for all $a, b, c \in L$, $a \vee b = 1 = a \vee c$ imply $a \vee (b \wedge c) = 1$. Of course, every distributive lattice with 0 and 1 is both 0-distributive and 1-distributive. A pseudo complemented lattice L can be characterized by the fact that for each $a \in L$, the set of all elements which are disjoint with element a forms a principal ideal. But a 0-distributive lattice L says that for each $a \in L$, the set of all elements which are disjoint with a is simply an ideal not necessarily a principal ideal. Hence, every pseudocomplemented lattice is 0-distributive. For detailed literature on 0-distributive lattice we refer the readers to consult [IV] and [I].

In this paper, we generalize the concept of 0-distributive lattice and n -distributive lattice and give the notion of n -distributive nearlattice where n is a central element of this nearlattice.

A nearlattice S is a meet semilattice with the property that, any two elements possessing a common upper bound, have a supremum. Nearlattice S is distributive if for all $x, y, z \in S, x \wedge (y \vee z) = (x \wedge y) \vee (x \wedge z)$ provided $y \vee z$ exists. For detailed literature on nearlattices, we refer the reader to consult [V] and [VIII]. An element n of a nearlattice S is called medial if $m(x, n, y) = (x \wedge y) \vee (x \wedge n) \vee (y \wedge n)$ exists in S for all $x, y \in S$. A nearlattice S is called a medial nearlattice if $m(x, y, z)$ exists for all $x, y, z \in S$.

An element s of a nearlattice S is called standard if for all $t, x, y \in S, t \wedge [(x \wedge y) \vee (x \wedge s)] = (t \wedge x \wedge y) \vee (t \wedge x \wedge s)$. The element s is called neutral if (i) s is standard and (ii) for all $x, y, z \in S, s \wedge [(x \wedge y) \vee (x \wedge z)] = (s \wedge x \wedge y) \vee (s \wedge x \wedge z)$.

In a distributive nearlattice, every element is neutral and hence standard. An element n in a nearlattice S is called sesquimedial if for all $x, y, z \in S, [(x \wedge n) \vee (y \wedge n)] \wedge [(y \wedge n) \vee (z \wedge n)] \vee (x \wedge y) \vee (y \wedge z)$ exists in S .

An element n of a nearlattice S is called an upper element if $x \vee n$ exists for all $x \in S$. Every upper element is of course a sesquimedial element. An element n is called a central element of S if it is neutral, upper and complemented in each interval containing it.

Let S be a nearlattice and $n \in S$. Any convex subnearlattice of S containing n is called an n -ideal of S . For two n -ideals I and J of a nearlattice S , [V] has given a description of $I \vee J$ while the set theoretic intersection is the infimum. Hence, the set of all n -ideals of a nearlattice S is a lattice which is denoted by $I_n(S)$. $\{n\}$ and S are the smallest and largest elements of $I_n(S)$.

An n -ideal generated by a finite number of elements a_1, a_2, \dots, a_m is called a finitely generated n -ideal and it is denoted by $\langle a_1, a_2, \dots, a_m \rangle_n$. The set of all finitely generated n -ideals is denoted by $F_n(S)$. Clearly, $\langle a_1, a_2, \dots, a_m \rangle_n = \langle a_1 \rangle_n \vee \langle a_2 \rangle_n \vee \dots \vee \langle a_m \rangle_n$. An n -ideal generated by a single element a is called a principal n -ideal denoted by $\langle a \rangle_n$. The set of principal n -ideals is denoted by $P_n(S)$.

Let S be a nearlattice and $n \in S$. For any $a \in S$,

$$\langle a \rangle_n = \{y \in S : a \wedge n \leq y = (y \wedge a) \vee (y \wedge n)\}$$

$= \{y \in S: y = (y \wedge a) \vee (y \wedge n) \vee (a \wedge n)\}$ whenever n is standard element in S .

If n is an upper element in a nearlattice S , then $\langle a \rangle_n = [a \wedge n, a \vee n]$.

We know that when n is standard and medial, the set of all principal n -ideals $P_n(S)$ is a meet semilattice and $\langle a \rangle_n \cap \langle b \rangle_n = \langle m(a, n, b) \rangle_n$ for all $a, b \in S$. Also, when n is neutral and sesquimedial, then $P_n(S)$ is a nearlattice. By [V] if S is medial nearlattice and n is a neutral element of S , then $P_n(S)$ is also a medial nearlattice.

For a distributive nearlattice S with an upper element n , $P_n(S)$ is a distributive nearlattice with the smallest element $\{n\}$.

A proper convex subnearlattice M of a nearlattice S is called a maximal convex subnearlattice if for any convex subnearlattice Q with $Q \supseteq M$ implies either $Q = M$ or $Q = S$. A proper convex subnearlattice M of a medial nearlattice S is called a prime convex subnearlattice if for any $t \in M, m(a, t, b) \in M$ implies either $a \in M$ or $b \in M$. For a medial element n , an n -ideal P of a nearlattice S is a prime n -ideal if $P \neq S$ and $m(x, n, y) \in P$ ($x, y \in S$) implies either $x \in P$ or $y \in P$. Equivalently, P is prime if and only if $\langle a \rangle_n \cap \langle b \rangle_n \subseteq P$ implies either $\langle a \rangle_n \subseteq P$ or $\langle b \rangle_n \subseteq P$.

Let n be a central element of a nearlattice S . For $a \in S$, we define $\{a\}^{\perp n} = \{x \in S: m(x, n, a) = n\}$, known as an n -annihilator of $\{a\}$. Also for $A \subseteq S$, we define $A^{\perp n} = \{x \in S: m(x, n, a) = n \text{ for all } a \in A\}$. $A^{\perp n}$ is always a convex subnearlattice containing n . If S is a distributive nearlattice, then it is easy to check $\{a\}^{\perp n}$ and $A^{\perp n}$ are n -ideals. Moreover, $A^{\perp n} = \bigcap_{a \in A} \{a\}^{\perp n}$. If A is an n -ideal, then $A^{\perp n}$ is called an annihilator n -ideal which is obviously the pseudocomplement of A in $I_n(S)$. Therefore, for a distributive nearlattice S with central element n , $I_n(S)$ is pseudocomplemented.

A nearlattice S with central element n , is called an n -distributive nearlattice if for all $a, b, c \in S, \langle a \rangle_n \cap \langle b \rangle_n = \{n\}$ and $\langle a \rangle_n \cap \langle c \rangle_n = \{n\}$ imply $\langle a \rangle_n \cap [\langle b \rangle_n \vee \langle c \rangle_n] = \{n\}$. Equivalently, S is called n -distributive nearlattice if $a \wedge b \leq n \leq a \vee b$ and $a \wedge c \leq n \leq a \vee c$ imply $a \wedge (b \vee c) \leq n \leq a \vee (b \wedge c)$.

II. Main results

To obtain the main results of this paper we need to prove the following lemmas.

Lemma (2.1): Every convex subnearlattice not containing n is contained in a maximal convex subnearlattice not containing n .

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Proof: Let F be a convex subnearlattice such that $n \notin F$. Let \mathcal{F} be the set of all convex subnearlattice containing F but not containing n . \mathcal{F} is non-empty as $F \in \mathcal{F}$. Let C be a chain in \mathcal{F} and $M = \cup (X | X \in C)$. Let $x, y \in M$. Then $x \in X$ and $y \in Y$ for some $X, Y \in C$. Since C is a chain, so either $X \subseteq Y$ or $Y \subseteq X$. Suppose $X \subseteq Y$. Then $x, y \in Y$. Hence $x \wedge y, x \vee y \in M$. Thus M is a subnearlattice of a nearlattice containing F . Also it is convex as each $X \in C$ is convex. Clearly $n \notin M$. Hence M is a maximal element of \mathcal{C} . Therefore, by Zorn's Lemma, \mathcal{F} has a maximal element, say Q with $F \subseteq Q$.

Lemma (2.2): Let S be a nearlattice with a central element n . A convex subnearlattice M not containing n is maximal if and only if for all $a \notin M$ there exists $b \in M$ such that $m(a, n, b) = n$.

Proof: Suppose M is a maximal convex subnearlattice and $n \notin M$. Also let $a \notin M$. Suppose for all $b \in M$, $m(a, n, b) \neq n$. Set $M_1 = \{y \in L : y \wedge n \leq (a \vee b) \leq (a \wedge b) \vee n \leq y \vee n\}$. Obviously, M_1 is convex subnearlattice as n is central. Moreover, $n \notin M_1$. For otherwise $n \wedge n \leq (a \vee b) \wedge n \leq (a \wedge b) \vee n \leq n \vee n$ implies $m(a, n, b) = n$ which gives a contradiction to the assumption. For $b \in M$, $b \wedge n \leq (a \vee b) \wedge n \leq (a \wedge b) \vee n \leq b \vee n$ implies $b \in M_1$ and so $M \subset M_1$. Also, $a \wedge n \leq (a \vee b) \wedge n \leq (a \wedge b) \vee n \leq a \vee n$ implies $a \in M_1$ but $a \notin M$ so $M \subset M_1$. Therefore, we have a contradiction to the maximality of M and so there exists some $b \in M$ such that $m(a, n, b) = n$. Conversely, if M is not maximal and $n \notin M$, then by **Lemma (2.1)**, M properly contained in a maximal convex subnearlattice N not containing n . Then for any element $a \in N - M$ there exists an element $b \in M$ such that $m(a, n, b) = n$. Thus, by convexity $a, b \in N$ and $a \wedge b \leq n \leq a \vee b$ imply $n \in N$ which is a contradiction. Hence, M must be maximal.

Following two lemmas are due to [VII]

Lemma(2.3): A proper subset I of a join semilattice S is a maximal ideal if and only if $S - I$ is a minimal prime up set (filter).

Lemma (2.4): Let I be an ideal of a join semilattice S with 1. Then there exists a maximal ideal containing I .

Theorem (2.5): For a medial element n , any prime ideal P containing n of a nearlattice S is a prime n -ideal.

Proof: Since every ideal P is a convex subnearlattice, so any ideal P containing n is an n -ideal. To show the primeness, let $m(a, n, b) \in P$. Then $a \wedge b \leq m(a, n, b)$ implies $a \wedge b \in P$. Since P is prime ideal so either $a \in P$ or $b \in P$. Hence P is a prime n -ideal.

Following lemma is due to [VI]

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Lemma (2.6): Every ideal disjoint from a filter F is contained in a maximal ideal disjoint from F .

Theorem(2.7): Let S be a nearlattice with a center element n . If the intersection of all prime n -ideals of S is $\{n\}$, then S is n -distributive.

Proof: Let $\langle a \rangle_n \cap \langle b \rangle_n = \{n\}$ and $\langle a \rangle_n \cap \langle c \rangle_n = \{n\}$. Let P be any prime n -ideal. If $a \in P$, then $\langle a \rangle_n \subseteq P$ and so $\langle a \rangle_n \cap [\langle b \rangle_n \vee \langle c \rangle_n] \subseteq P$. If $a \notin P$, then $\langle b \rangle_n, \langle c \rangle_n \subseteq P$ as P is prime n -ideal. Hence $\langle b \rangle_n \vee \langle c \rangle_n \subseteq P$. Therefore, $\langle a \rangle_n \cap [\langle b \rangle_n \vee \langle c \rangle_n] \subseteq P$. That is, in either case, $\langle a \rangle_n \cap [\langle b \rangle_n \vee \langle c \rangle_n] \subseteq P$ for all prime n -ideals P . Therefore, $\langle a \rangle_n \cap [\langle b \rangle_n \vee \langle c \rangle_n] = \{n\}$ and so S is n -distributive.

Lemma (2.8): Let S be a nearlattice with a central element n . Then $p \in \{x\}^{\perp n}$ if and only if $p \wedge x \leq n \leq p \vee x$.

Proof: $p \in \{x\}^{\perp n}$ if and only if $m(p, n, x) = n$ if and only if $(p \wedge x) \vee (p \wedge n) \vee (x \wedge n) = (p \vee x) \wedge (p \vee n) \wedge (x \vee n) = n$, as n is central. This implies that $p \wedge x \leq n \leq p \vee x$.

Lemma (2.9): Let S be a nearlattice with a central element n . Then $p \in \{x\}^{\perp n}$ if and only if $p \vee n \in \{x \vee n\}^{\perp n}$ in $[n]$ and $p \wedge n \in \{x \wedge n\}^{\perp d}$ in (n) .

Proof: Let $p \in \{x\}^{\perp n}$. Then $p \wedge x \leq n \leq p \vee x$ and so $(p \vee n) \wedge (x \vee n) = (p \wedge x) \vee n = n$ and $(p \wedge n) \vee (x \wedge n) = (p \vee x) \wedge n = n$ as n is central element. Thus $p \vee n \in \{x \vee n\}^{\perp}$ in $[n]$ and $p \wedge n \in \{x \wedge n\}^{\perp d}$ in (n) . Conversely, let $p \vee n \in \{x \vee n\}^{\perp}$ in $[n]$ and $p \wedge n \in \{x \wedge n\}^{\perp d}$ in (n) . Then since n is central element, so $(p \vee n) \wedge (x \vee n) = n$ and $(p \wedge x) \vee n = n$. This implies $p \wedge x \leq n$. Also, $(p \wedge n) \vee (x \wedge n) = n$ implies $(p \vee x) \wedge n = n$ and so $n \leq p \vee x$. Hence $p \wedge x \leq n \leq p \vee x$. Therefore, by **Lemma (2.8)**, $p \in \{x\}^{\perp n}$.

Now, we give some characterizations of n -distributive nearlattices.

Theorem (2.10): For a nearlattice S with a central element n , the following conditions are equivalent:

- (i) S is n -distributive
- (ii) For every $a \in S$, $\{a\}^{\perp n}$ is an n -ideal
- (iii) For any $A \subseteq S$, $A^{\perp n}$ is an n -ideal
- (iv) $I_n(S)$ is pseudocomplemented.
- (v) $I_n(S)$ is 0-distributive
- (vi) Every maximal convex subnearlattice not containing n is prime.

Proof: (i) \Rightarrow (ii). Let $x, y \in \{a\}^{\perp n}$. Then $a \wedge x \leq n \leq a \vee x$ and $a \wedge y \leq n \leq a \vee y$. Since S is distributive, so $a \wedge (x \vee y) \leq n \leq a \vee (x \wedge y)$. Then $a \wedge (x \vee y) \leq n \leq a \vee (x \wedge y)$ and $a \wedge (x \wedge y) \leq n \leq a \vee (x \vee y)$ imply $x \wedge y, x \vee y \in \{a\}^{\perp n}$ [by

Lemma (2.8)]. Since $m(x, n, a) = n$, so $n \in \{a\}^{\perp n}$.

Again, let $x, y \in \{a\}^{\perp n}$ and $x \leq t \leq y$. Then $a \wedge x \leq n \leq a \vee x$ and $a \wedge y \leq n \leq a \vee y$ so $a \wedge t \leq n \leq a \vee t$ which implies that $t \in \{a\}^{\perp n}$. Hence $\{a\}^{\perp n}$ is an n -ideal.

(ii) \Rightarrow (iii). Since $\{a\}^{\perp n}$ is an n -ideal and $A^{\perp n} = \bigcap_{a \in A} \{\{a\}^{\perp n}\}$, so $A^{\perp n}$ is an n -ideal.

(iii) \Rightarrow (iv) is trivial as for any n -ideal $A \in I_n(S)$, $A^{\perp n}$ is the pseudocomplement of A in $I_n(S)$.

(iv) \Rightarrow (v) is also trivial because every pseudocomplemented lattice is 0-distributive.

(v) \Rightarrow (vi). Suppose F is maximal convex subnearlattice not containing n . Since $F = (F) \cap [F]$ and $n \in F$, so either $n \notin (F)$ or $n \notin [F]$. Hence by the maximality of F , either F is an ideal or a filter. Let $x \notin F$ and $y \notin F$. Then by **Lemma (2.2)**, there exist $a \in F$ and $b \in F$ such that $m(x, n, a) = n = m(y, n, b)$. This implies $x \wedge a \leq n \leq x \vee a$ and $y \wedge b \leq n \leq y \vee b$. Hence $x \wedge a \wedge b \leq n, y \wedge a \wedge b \leq n$ and $x \vee a \vee b \geq n, y \vee a \vee b \geq n$ and so $a \wedge b, a \vee b \in F$. Then $\langle x \vee n \rangle_n \cap \langle a \wedge b \rangle_n = [n, x \vee n] \cap [a \wedge b \wedge n, (a \wedge b) \vee n]$

$$= [n, (x \wedge a \wedge b) \vee n] = [n, n] = \{n\} \text{ as } n \text{ is central.}$$

Similarly, $\langle y \vee n \rangle_n \cap \langle a \wedge b \rangle_n = \{n\}$. Since $I_n(S)$ 0-distributive, so $\langle a \wedge b \rangle_n \cap (\langle x \vee n \rangle_n \vee \langle y \vee n \rangle_n) = \{n\}$. This implies $[n, (a \wedge b \wedge (x \vee y)) \vee n] = \{n\}$. Hence $a \wedge b \wedge (x \vee y) \leq n$. Dually, $\langle x \wedge n \rangle_n \cap \langle a \vee b \rangle_n = \{n\}$ and $\langle y \wedge n \rangle_n \cap \langle a \vee b \rangle_n = \{n\}$. Without loss of generality, suppose F is filter. If $x \vee y \in F$, then $a \wedge b \wedge (x \vee y) \leq n$ implies $n \in F$ which is a contradiction. Hence $x \vee y \notin F$. Therefore, F is prime filter. Similarly, if F is an ideal, then it is a prime ideal

(vi) \Rightarrow (i). Let $a \wedge b \leq n \leq a \vee b$ and $a \wedge c \leq n \leq a \vee c$ provided $a \vee b$ and $a \vee c$ exist. We need to show that $a \wedge (b \vee c) \leq n \leq a \vee (b \wedge c)$. If not, without loss of generality, let $a \wedge (b \vee c) \notin n$. Consider $F = [a \wedge (b \vee c)]$, when $b \vee c$ exists. So $n \notin F$. Then by Lemma 1, there exists maximal convex subnearlattice $M \supseteq F$ and $n \notin M$. But a convex subnearlattice containing a filter is itself a filter. Then by (vi), M is a filter. Now, $a \in M$ and $b \vee c \in M$ imply $a \wedge b \in M$ or $a \wedge c \in M$ as M is prime. This implies $n \in M$ which is a contradiction. Hence $a \wedge (b \vee c) \leq n \leq a \vee (b \wedge c)$. Therefore, S is n -distributive.

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Corollary(2.11): In an n -distributive nearlattice every filter not containing n is contained in a prime filter.

Proof: This is trivial by **Lemma (2.1)** and **Theorem (2.10)**.

Theorem (2.12): Let S be an n -distributive nearlattice. If $A \neq \{n\}$ and $A = \bigcap \{I \in I_n(S) : I \neq \{n\}\}$, then $A^{\perp n} = \{x \in S : \{x\}^{\perp n} \neq \{n\}\}$.

Proof: Let $x \in A^{\perp n}$. Then $m(x, n, a) = n$ for all $x \in A$. Since $A \neq \{n\}$ so $\{x\}^{\perp n} \neq \{n\}$. Hence $x \in R.H.S.$ So $A^{\perp n} \subseteq R.H.S.$ Conversely, let $x \in R.H.S.$ Since S is n -distributive so $\{x\}^{\perp n}$ is an n -ideal and so $\{x\}^{\perp n} \neq \{n\}$. Then $A \subseteq \{x\}^{\perp n}$ and so $A^{\perp n} \supseteq \{x\}^{\perp n}$. Therefore, $A^{\perp n} = \{x \in S : \{x\}^{\perp n} \neq \{n\}\}$.

Theorem (2.13): Let S be a nearlattice with a central element n . Then S is n -distributive if and only if for a convex subnearlattice F disjoint with $\{x\}^{\perp n} (x \in S)$, there exists a prime convex subnearlattice $P \supseteq F$ and disjoint with $\{x\}^{\perp n}$.

Proof: Let S be n -distributive and F be a convex subnearlattice disjoint from $\{x\}^{\perp n}$. Then by Zorn's Lemma, there exists a maximal convex subnearlattice P disjoint from $\{x\}^{\perp n}$. Since $P = (P) \cap [P]$ so either $(P) \cap \{x\}^{\perp n} = \phi$ or $[P] \cap \{x\}^{\perp n} = \phi$. Thus by the maximality of P , it is either an ideal or a filter. Without loss of generality, let P be a filter. We claim that $x \in P$. If not $P \vee [x] \supset P$. Then by the maximality of P , $(P \vee [x]) \cap \{x\}^{\perp n} \neq \phi$. Let $t \in (P \vee [x]) \cap \{x\}^{\perp n}$. Then $t \geq p \wedge x$ for some $p \in P$ and $t \wedge x \leq n \leq t \vee x$. Thus $p \wedge x \leq t \wedge x \leq n$. hence $m(p \vee n, n, x) = n$ which implies $p \vee n \in \{x\}^{\perp n}$. But $p \vee n \in P$ as P is a filter. This gives a contradiction to the fact that $P \cap \{x\}^{\perp n} = \phi$. Therefore $x \in P$. Let $z \notin P$, then $(P \vee [z]) \cap \{x\}^{\perp n} \neq \phi$. Let $y \in (P \vee [z]) \cap \{x\}^{\perp n}$. Then $y \wedge x \leq n \leq y \vee x$ and $y \geq p_1 \wedge z$ for some $p_1 \in P$ so $p_1 \wedge x \wedge z \leq y \wedge x \leq n$. Hence $m(z, n, (p_1 \wedge x) \vee n) = n$ where $(p_1 \wedge x) \vee n \in P$ as P is a filter. Then by **Lemma (2.2)**, P is a maximal filter not containing n . Therefore, by **Theorem (2.10)**, P is Prime.

Conversely, let $\langle x \rangle_n \cap \langle y \rangle_n = \{n\}$ and $\langle x \rangle_n \cap \langle z \rangle_n = \{n\}$. We need to prove that $\langle x \rangle_n \cap (\langle y \rangle_n \vee \langle z \rangle_n) = \{n\}$. That is, $x \wedge (y \vee z) \not\leq n$. Then $[y \vee z] \cap \{x\}^{\perp n} = \phi$. Otherwise $t \in [y \vee z] \cap \{x\}^{\perp n}$ implies $t \wedge x \leq n \leq t \vee x$ and $t \geq y \vee z$. These imply $x \wedge (y \vee z) \leq t \wedge x \leq n$ is a contradiction. So there exists a prime filter P containing $[y \vee z]$ disjoint with $\{x\}^{\perp n}$. Since $z \in \{x\}^{\perp n}$ so $y, z \notin P$. Hence $y \vee z \notin P$ as P is a prime filter. This implies $P \not\supseteq [y \vee z]$ is a contradiction. Dually by taking $x \vee (y \wedge z) \not\leq n$, we would have another contradiction. Therefore, $x \wedge (y \vee z) \leq n \leq x \vee (y \wedge z)$ and so S is n -distributive.

III. Conclusion

In this paper, we generalize the concept of 0-distributive lattice and n -distributive lattice where n is a neutral element of this lattice and give the notion of n -distributive nearlattice where n is a central element of this nearlattice. We also include several nice characterizations of n -distributive nearlattices and prove some interesting results on n -distributive nearlattices.

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